

Show all work clearly and in order, and circle your final answers. Justify your answers algebraically whenever possible; when you do use your calculator, sketch all relevant graphs and write down all relevant mathematics. You have 15 minutes to take this 15 point quiz.

**Important: Only final answers written in the blank will receive points,**

**1.** (10 points)  $(2 + 2 + 1 \times 6)$  Fill in the blanks,

1. How many relations are there on the set  $\{a, b, c, d\}$ ?  $2^{16}$  \_\_\_\_\_
2. How many relations are there on the set  $\{a, b, c, d\}$  that contain the pair  $(a, a)$ ?  $2^{15}$  \_\_\_\_\_
3. Consider the relation  $R = \{(2, 2), (2, 3), (2, 4), (3, 2), (3, 3), (3, 4)\}$  on the set  $A = \{1, 2, 3, 4\}$ . Is it ?
  - (a) reflexive? F \_\_\_\_\_
  - (b) irreflexive? F \_\_\_\_\_
  - (c) symmetric? F \_\_\_\_\_
  - (d) antisymmetric? F \_\_\_\_\_
  - (e) asymmetric? F \_\_\_\_\_
  - (f) transitive? T \_\_\_\_\_

**2.** (5 points) Let  $R$  be the relation  $\{(a, b), \text{ such that } a \text{ divides } b\}$  on the set of integers. What is the symmetric closure of  $R$ ?

**Final answer here:**  $R \cup R^{-1} = \{(a, b) : a|b \text{ or } b|a\}$  \_\_\_\_\_